

MCS 107 MT2 Questions

1) Given the function $f(x) = 4 + x - 2x^2 - 4x^3$

- a) Find the intervals of increasing and decreasing
- b) Find local maximum and minimum points
- c) Find the intervals of concavity and inflection points

2) Find $f'(x)$, if

a) $f(x) = \log_4(x+2)^5$ b) $f(x) = (16x+76)e^{4x+9}$ c) $f(x) = \sqrt{3x+1} + 2^{3x+1}$

3) The total revenue from the sales of a certain product are given by $R(x) = \frac{20x}{\ln(3x+4)}$.

Find the marginal revenue.

4) Let $f(x) = \begin{cases} x^3 - 8 & : x \leq -1 \\ 4x - 2 & : -1 < x \leq 1 \\ 2 & : x > 1 \end{cases}$

- a) Find $f(-1)$ and $f(\frac{1}{2})$
- b) Is f continuous at $x = -1$ and $x = 1$?
- c) Find $f'(1)$ (if exists)

5) Given $f(x) = (x^2 + 3)e^{-x}$.

- a) Find $f'(0)$
- b) Find equation of tangent line at $(0, 3)$

6) Evaluate

a) $\lim_{x \rightarrow 1} \frac{1+x-2x^2}{3x^2+2x-5}$ b) $\lim_{x \rightarrow \infty} \frac{1+x-2x^2}{3x^2+2x-5}$ c) $\lim_{x \rightarrow 2} \frac{\sqrt{3x+10}-4}{x-2}$